

CHAPTER TEST: TRIANGLES (SET-B)

Mathematics — Class IX (2026/TRIANG/09/002)

Time: 1.5 Hours

Max. Marks: 40

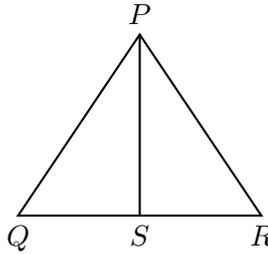
General Instructions:

- All questions are compulsory.
- Section A: 8 MCQs (1 Mark each).
- Section B: 4 Very Short Questions (2 Marks each).
- Section C: 3 Short Questions (3 Marks each).
- Section D: 2 Long Questions (5 Marks each).
- Section E: 1 Case Study (5 Marks).

Section A: Multiple Choice Questions ($8 \times 1 = 8$ Marks)

1. In $\triangle ABC$ and $\triangle PQR$, if $AB = PQ$, $BC = QR$ and $\angle B = \angle Q$, then the triangles are congruent by:
 - (a) SSS Rule
 - (b) SAS Rule
 - (c) ASA Rule
 - (d) RHS Rule
2. If the altitudes from two vertices of a triangle to the opposite sides are equal, then the triangle is:
 - (a) Scalene
 - (b) Isosceles
 - (c) Right-angled
 - (d) Equilateral
3. In $\triangle ABC$, $AB = AC$ and $\angle B = 50^\circ$. Then $\angle C$ is:
 - (a) 40°
 - (b) 50°
 - (c) 80°
 - (d) 130°
4. In a $\triangle ABC$, if $AB = 5$ cm and $BC = 7$ cm, then the third side AC must satisfy:
 - (a) $AC < 2$ cm
 - (b) $AC > 12$ cm
 - (c) $2 \text{ cm} < AC < 12 \text{ cm}$
 - (d) $AC = 12$ cm

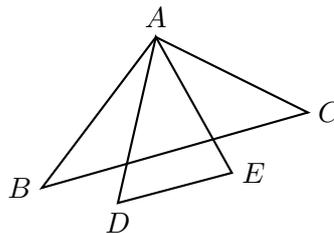
5. In the given figure, PS is the bisector of $\angle QPR$ and $PQ = PR$. Then $\triangle PQS \cong \triangle PRS$ by:



- (a) SAS
(b) SSS
(c) RHS
(d) ASA
6. If the angles of a triangle are in the ratio $1 : 2 : 3$, the triangle is:
- (a) Isosceles
(b) Equilateral
(c) Right-angled
(d) Obtuse-angled
7. In $\triangle PQR$, if $\angle R > \angle Q$, then:
- (a) $QR > PR$
(b) $PQ > PR$
(c) $PQ < PR$
(d) $QR < PR$
8. The perimeter of a triangle is _____ the sum of its three medians.
- (a) Equal to
(b) Less than
(c) Greater than
(d) Half of

Section B: Very Short Answer Questions ($4 \times 2 = 8$ Marks)

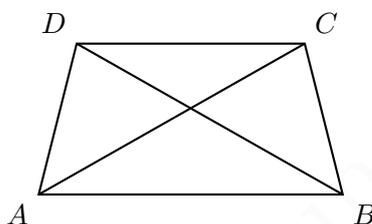
1. In the given figure, $AC = AE$, $AB = AD$ and $\angle BAD = \angle EAC$. Show that $BC = DE$.



- If two sides of a triangle are 8 cm and 11 cm, and the perimeter is 32 cm, find the third side. Is it possible for this triangle to be a right-angled triangle?
- Prove that each angle of an equilateral triangle is 60° .
- In $\triangle ABC$, $\angle A = 100^\circ$ and $AB = AC$. Calculate $\angle B$ and $\angle C$.

Section C: Short Answer Questions ($3 \times 3 = 9$ Marks)

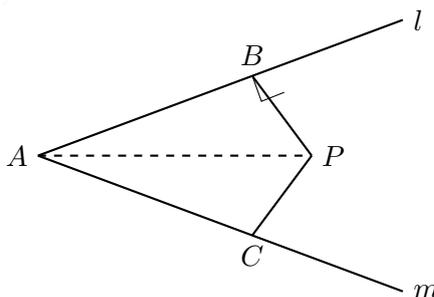
- $ABCD$ is a quadrilateral in which $AD = BC$ and $\angle DAB = \angle CBA$. Prove that:
 - $\triangle ABD \cong \triangle BAC$
 - $BD = AC$
 - $\angle ABD = \angle BAC$



- Prove that the sum of any two sides of a triangle is greater than the third side.
- In $\triangle ABC$, AD is the bisector of $\angle A$. If $AB > AC$, prove that $\angle ADB > \angle ADC$.

Section D: Long Answer Questions ($2 \times 5 = 10$ Marks)

- P is a point equidistant from two lines l and m intersecting at point A . Show that the line AP bisects the angle between them.



- ABC is a triangle in which $\angle B = 2\angle C$. D is a point on BC such that AD bisects $\angle BAC$ and $AB = CD$. Prove that $\angle BAC = 72^\circ$.

Section E: Case Study Based Question ($1 \times 5 = 5$ Marks)

Case Study:

A civil engineer is designing a pedestrian bridge across a small stream. The structural support of the bridge is based on a triangular truss system. The main support is an isosceles triangle ABC with $AB = AC$. To strengthen the bridge, the engineer adds two points D and E on the base BC such that $AD \perp BC$ and AE is a median to the side BC . During a safety audit,

the inspector needs to verify the congruence of various triangles to ensure the load is balanced. The total length of the base BC is 20 meters, and the height of the apex A from the base is 10 meters. The engineer claims that the symmetry of the design reduces material costs while maintaining maximum safety.

1. In the isosceles $\triangle ABC$, if $\angle B = 65^\circ$, find the measure of the vertex angle $\angle A$.
 - (a) 65°
 - (b) 130°
 - (c) 50°
 - (d) 60°
2. Since $AD \perp BC$ in an isosceles triangle ABC (where $AB = AC$), what is the relationship between BD and DC ?
 - (a) $BD > DC$
 - (b) $BD < DC$
 - (c) $BD = DC$
 - (d) No fixed relation
3. Which congruence rule proves $\triangle ABD \cong \triangle ACD$?
 - (a) SSS
 - (b) RHS
 - (c) AAA
 - (d) SAS only
4. If the engineer moves point A such that $AB \neq AC$, which property will be lost?
 - (a) The sum of interior angles is 180°
 - (b) The triangle inequality $AB + BC > AC$
 - (c) Symmetry and equality of base angles
 - (d) None of the above
5. If a new support is added joining the midpoint of AB to the midpoint of AC , this line will be:
 - (a) Perpendicular to BC
 - (b) Parallel to BC
 - (c) Intersecting BC at 45°
 - (d) Equal to BC