

Solutions: Algebraic Expressions

1.

$$\begin{aligned}
 A - B + C &= (2m^2 - 5mn + n^2) - (-3m^2 + 4mn - 2n^2) + (m^2 + 3mn + n^2) \\
 &= 2m^2 - 5mn + n^2 + 3m^2 - 4mn + 2n^2 + m^2 + 3mn + n^2 \\
 &= (2m^2 + 3m^2 + m^2) + (-5mn - 4mn + 3mn) + (n^2 + 2n^2 + n^2) \\
 &= 6m^2 + 2mn + 4n^2
 \end{aligned}$$

The value of $A - B + C$ is $6m^2 + 2mn + 4n^2$.

2. The coefficients of x^2y and xy^2 are 7 and -4, respectively.

$$7 + (-4) = 3$$

The sum of the coefficients is 3.

3. Let the expression to be subtracted be E :

$$(10p - 7q + 15r) - E = -2p + 3q - 8r$$

$$E = (10p - 7q + 15r) - (-2p + 3q - 8r) = 12p - 10q + 23r$$

The expression to be subtracted is $12p - 10q + 23r$.

4.

$$\begin{aligned}
 \frac{1}{3}(9a - 6b + 12) &= 3a - 2b + 4 \\
 \frac{1}{2}(4a + 2b - 8) &= 2a + b - 4 \\
 (3a - 2b + 4) - (2a + b - 4) &= a - 3b + 8
 \end{aligned}$$

The simplified expression is $a - 3b + 8$.

5. Like terms have the same variables raised to the same powers. The pair $-11p^2q$ and $7qp^2$ are like terms. The correct pair is $-11p^2q$ and $7qp^2$.

6. The perimeter P of a rectangle is given by:

$$P = 2 \times (\text{length} + \text{breadth}) = 2 \times (5k + 2 + 3k - 1) = 2 \times (8k + 1) = 16k + 2$$

The algebraic expression for the perimeter is $16k + 2$ units.

7.

$$(2x^2 - 8) + (-3x^2 + 5x + 10) + (x^2 - 5x - 1) = (2x^2 - 3x^2 + x^2) + (5x - 5x) + (-8 + 10 - 1) = 0x^2 + 0x + 1$$

The constant term is 1.

8.

$$-1 \times (3u^2v - 2uv^2) = -3u^2v + 2uv^2$$

$$(-3u^2v + 2uv^2) + (-5u^2v + 7uv^2) = -8u^2v + 9uv^2$$

The result is $[-8u^2v + 9uv^2]$.

9. Simplify inside the brackets:

$$5b - 6a - 7b = -6a - 2b$$

$$4a - (-6a - 2b) = 4a + 6a + 2b = 10a + 2b$$

$$3b - (10a + 2b) = 3b - 10a - 2b = -10a + b$$

$$2a - (-10a + b) = 2a + 10a - b = 12a - b$$

The simplified expression is $[-8a - 5b]$.

10. The correct statement is: It has two variable terms and one constant term. The correct option is **[D]**.

11.

$$(12x + 50) - (4x - 25) - (3x + 15) = 12x + 50 - 4x + 25 - 3x - 15 = 5x + 60$$

The simplified expression for the money left is $[Rs.(5x + 60)]$.

12.

$$(5.2a^2 + 0.8a^2) + (-3.1a - a) + 4 = 6a^2 - 4.1a + 4$$

The number of terms is **[3]**.

13.

$$(-2f^2 + 5fg) + (3f^2 - 8fg) = f^2 - 3fg$$

$$(4f^2 - fg) - (f^2 - 3fg) = 3f^2 + 2fg$$

The result is $[3f^2 + 2fg]$.

14.

$$\frac{3x + 7}{2}$$

The algebraic expression is $\left[\frac{3x + 7}{2}\right]$.

15. The expression $7m - 6n + 0$ has a constant term of 0. The correct option is **[7m - 6n + 0]**.