

Solutions: Algebraic Expressions

1.

$$\begin{aligned} (-3x^2y) \times (2xy - 5y^2) &= (-3x^2y \times 2xy) + (-3x^2y \times -5y^2) \\ &= -6x^3y^2 + 15x^2y^3 \end{aligned}$$

The product is $[-6x^3y^2 + 15x^2y^3]$.

2.

$$\begin{aligned} (7a^2 - 3ab + b^2) + (-2a^2 + ab - 4b^2) + (a^2 + 2ab + 3b^2) \\ = (7a^2 - 2a^2 + a^2) + (-3ab + ab + 2ab) + (b^2 - 4b^2 + 3b^2) \\ = 6a^2 + 0ab + 0b^2 = 6a^2 \end{aligned}$$

The sum is $[6a^2]$.3. The pair $4x^2y^2$ and $4x^2y$ are unlike terms because the exponents of y are different.The correct option is $[4x^2y^2 \text{ and } 4x^2y]$.

4.

$$\text{Third side} = (15x + 12) - (4x + 5 + 5x - 3) = 6x + 10$$

The third side is $[6x + 10]$.

5.

$$\begin{aligned} 4q - (5p - 6q) &= 4q - 5p + 6q = -5p + 10q \\ 3p - (-5p + 10q) &= 3p + 5p - 10q = 8p - 10q \\ 2(8p - 10q) &= 16p - 20q \\ (16p - 20q) - (p - 2q) &= 15p - 18q \end{aligned}$$

The simplified form is $[15p - 18q]$.

6.

$$\begin{aligned} 2A &= 2(5x - 3y + 2) = 10x - 6y + 4 \\ 3B &= 3(2x + 4y - 5) = 6x + 12y - 15 \\ 2A - 3B &= (10x - 6y + 4) - (6x + 12y - 15) = 4x - 18y + 19 \end{aligned}$$

The result is $[4x - 18y + 19]$.7. The expression $\frac{5x}{2} - \frac{3y}{4} + 7$ has three terms. The number of terms is $[3]$.8. Let the expression to be added be E :

$$(9m^2 - 4mn + n^2) + E = 3m^2 + 2mn - 5n^2$$

$$E = (3m^2 + 2mn - 5n^2) - (9m^2 - 4mn + n^2) = -6m^2 + 6mn - 6n^2$$

The expression to be added is $[-6m^2 + 6mn - 6n^2]$.

9. The coefficient of xy is $-\frac{2}{5}$. The coefficient is $-\frac{2}{5}$.

10.

$$(15x + 40) - (7x - 15 + 3x + 10) = 15x + 40 - 10x - 5 = 5x + 35$$

The money left is Rs.(5x + 35).

11.

$$(0.2a^2b + 0.8a^2b) + (-0.5ab^2 + 0.3ab^2) = 1.0a^2b - 0.2ab^2$$

The simplified form is 1.0a²b - 0.2ab².

12. The expression $a^2 + ab + b^2$ is a trinomial with no constant term. The correct option is $a^2 + ab + b^2$.

13.

$$(5p^2q + 2pq^2) - (p^2q - pq^2) = 4p^2q + 3pq^2$$

$$(8p^2q - 3pq^2) + (4p^2q + 3pq^2) = 12p^2q + 0pq^2 = 12p^2q$$

The sum is 12p²q.

14.

$$\text{Perimeter} = 4 \times (3x - 4) = 12x - 16$$

The perimeter is 12x - 16 units.

15. The incorrect statement is: $-2x^2$ and $\frac{3x}{5}$ are like terms. The correct option is $-2x^2$ and $\frac{3x}{5}$ are like terms.