

## Solutions: Algebraic Expressions

1.

$$(8xy^2 + 2x^2y - 4) - (5x^2y - 3xy^2 + 7) = (8xy^2 + 3xy^2) + (2x^2y - 5x^2y) + (-4 - 7) = 11xy^2 - 3x^2y - 11$$

The coefficient of  $xy^2$  is 11.

2. Let the base be  $B$ . The perimeter is the sum of all sides:

$$2(2a+b) + B = 7a + 5b \implies 4a + 2b + B = 7a + 5b \implies B = 7a + 5b - 4a - 2b = 3a + 3b$$

The expression for the base is 3a + 3b.

3. Unlike terms have different variables or exponents.  $4m^2n$  and  $4mn^2$  are unlike terms because the exponents of  $m$  and  $n$  are different. The correct pair is 4m<sup>2</sup>n and 4mn<sup>2</sup>.

4.

$$\begin{aligned} 0.5(4x^2 - 6x + 8) &= 2x^2 - 3x + 4 \\ -2(1.5x - x^2 + 1) &= -3x + 2x^2 - 2 \end{aligned}$$

Combining both:

$$(2x^2 + 2x^2) + (-3x - 3x) + (4 - 2) = 4x^2 - 6x + 2$$

The simplified expression is 4x<sup>2</sup> - 6x + 2.

5.

$$\begin{aligned} 2P &= 2(3x^2 - 4xy + 9) = 6x^2 - 8xy + 18 \\ -3Q &= -3(-2x^2 + 6xy - 5) = 6x^2 - 18xy + 15 \end{aligned}$$

Adding both:

$$(6x^2 + 6x^2) + (-8xy - 18xy) + (18 + 15) = 12x^2 - 26xy + 33$$

The value of  $2P - 3Q$  is 12x<sup>2</sup> - 26xy + 33.

6. The coefficients of the terms containing variables are 2, 3, 4, 5. Their sum is:

$$2 + 3 + 4 + 5 = 14$$

The sum of the coefficients is 14.

7. Let the expression to be added be  $E$ :

$$(7p^2 - 8pq + 4q^2) + E = 10pq - 3p^2 + 2q^2$$

$$E = (10pq - 3p^2 + 2q^2) - (7p^2 - 8pq + 4q^2) = -10p^2 + 18pq - 2q^2$$

The expression to be added is -10p<sup>2</sup> + 18pq - 2q<sup>2</sup>.

8. Sum of  $2m + 7n - 4$  and  $4m - 2n + 1$ :

$$(2m + 4m) + (7n - 2n) + (-4 + 1) = 6m + 5n - 3$$

Subtracting  $5m - 3n + 8$ :

$$(6m - 5m) + (5n + 3n) + (-3 - 8) = m + 8n - 11$$

The result is  $m + 6n - 5$ .

9.

$$\frac{1}{2} \times 3x \times (2x + 5 + x - 2) = \frac{1}{2} \times 3x \times (3x + 3) = \frac{3x(3x + 3)}{2} = \frac{9x^2 + 9x}{2}$$

The simplified expression is  $\frac{9x^2 + 9x}{2}$  sq. units.

10. The false statement is:  $3x^2y$  and  $7xy^2$  are like terms. The correct answer is Option D.

11.

$$(0.2a^2b + 3.4a^2b - 0.8a^2b) + (-1.5ab^2 + 2.1ab^2) = 2.8a^2b + 0.6ab^2$$

The simplified expression is  $2.8a^2b + 0.6ab^2$ .

12. Let the other expression be  $E$ :

$$(3l^2 + 5lm - 6m^2) + E = 9l^2 - 4lm + 2m^2$$

$$E = (9l^2 - 4lm + 2m^2) - (3l^2 + 5lm - 6m^2) = 6l^2 - 9lm + 8m^2$$

The other expression is  $6l^2 - 9lm + 8m^2$ .

13.

$$5(3x + 10) + 3(x - 4) = 15x + 50 + 3x - 12 = 18x + 38$$

The total cost is Rs.(18x + 38).

14. Simplify inside the brackets:

$$3q - (4r - p) = 3q - 4r + p$$

$$2p - [3q - 4r + p] = 2p - 3q + 4r - p = p - 3q + 4r$$

$$- \{p - 3q + 4r + 5r\} = -p + 3q - 9r$$

The equivalent expression is  $-p + 3q - 9r$ .

15. The numerical coefficients of the terms containing variables are  $\frac{5}{2}$  and  $-\frac{3}{4}$ . Their sum is:

$$\frac{5}{2} - \frac{3}{4} = \frac{10}{4} - \frac{3}{4} = \frac{7}{4} = 1.75$$

The sum of the numerical coefficients is 1.75.