

## Solutions: Algebraic Expressions

1.

$$\begin{aligned}
 & (0.6x^2y - 1.2xy^2) - (0.3x^2y + 0.8xy^2) + (1.5xy^2 - 0.9x^2y) \\
 &= 0.6x^2y - 1.2xy^2 - 0.3x^2y - 0.8xy^2 + 1.5xy^2 - 0.9x^2y \\
 &= (0.6x^2y - 0.3x^2y - 0.9x^2y) + (-1.2xy^2 - 0.8xy^2 + 1.5xy^2) \\
 &= -0.6x^2y + 0.5xy^2
 \end{aligned}$$

The simplified form is  $-0.6x^2y + 0.5xy^2$ .

2.

$$\begin{aligned}
 3(5a - 3b + 2c) &= 15a - 9b + 6c \\
 (15a - 9b + 6c) - (2a + 4b - c) &= 13a - 13b + 7c
 \end{aligned}$$

The final expression is  $13a - 13b + 7c$ .

3. The expression  $3y - 8$  is a binomial with a constant term of  $-8$ . The correct option is  $3y - 8$ .

4.

$$\text{Length} = \frac{\text{Area}}{\text{Width}} = \frac{12k^2 + 5k - 2}{3k + 2}$$

Performing polynomial division or factoring:

$$12k^2 + 5k - 2 = (3k + 2)(4k - 1)$$

The expression for the length is  $4k - 1$ .

5.

$$\begin{aligned}
 \frac{1}{4}(16p - 12q + 8) &= 4p - 3q + 2 \\
 \frac{2}{3}(9q - 6p + 3) &= 6q - 4p + 2 \\
 (4p - 3q + 2) + (6q - 4p + 2) &= 3q + 4
 \end{aligned}$$

The coefficient of  $p$  in the sum is  $0$ .

6.

$$3m^2 - 5m$$

The correct algebraic expression is  $3m^2 - 5m$ .

7.

$$(7x^2y - 4xy^2) + P = 2x^2y + 3xy^2$$

$$P = (2x^2y + 3xy^2) - (7x^2y - 4xy^2) = -5x^2y + 7xy^2$$

The expression for  $P$  is  $-5x^2y + 7xy^2$ .

8.

$$4b - 5a + 6b = -5a + 10b$$

$$3a - (-5a + 10b) = 3a + 5a - 10b = 8a - 10b$$

$$2b + (8a - 10b) = 8a - 8b$$

$$5a - (8a - 8b) = -3a + 8b$$

The simplified form is  $\boxed{3a - 8b}$ .

9. The numerical coefficient of the second term  $\frac{7}{10}bc$  is  $\boxed{\frac{7}{10}}$ .

10.

$$\text{Third side} = (15m + 21) - (4m + 5 + 5m + 8) = 6m + 8$$

The length of the third side is  $\boxed{6m + 8}$ .

11.

$$2(2r^2s + rs^2) = 4r^2s + 2rs^2$$

$$(8r^2s - 3rs^2) - (4r^2s + 2rs^2) = 4r^2s - 5rs^2$$

The difference is  $\boxed{4r^2s - 5rs^2}$ .

12. The expression  $m + n = 10$  is not a valid algebraic expression because it contains an equality sign. The correct option is  $\boxed{m + n = 10}$ .

13.

$$\text{Perimeter} = 2[(2x + 7) + (x - 3)] = 2(3x + 4) = 6x + 8$$

$$\text{Half of perimeter} = \frac{6x + 8}{2} = 3x + 4$$

The expression for half of the perimeter is  $\boxed{(3x + 4)}$  cm.

14. The expression  $9 - 5u + 2u^2$  has the constant term 9, the coefficient of  $u$  is  $-5$ , and the coefficient of  $u^2$  is 2. The correct option is  $\boxed{\text{The constant term 9, coefficient of } u \text{ is } -5, \text{ and coefficient of } u^2 \text{ is 2}}$ .

15.

$$\frac{3x - 4y}{2} = \frac{12x - 16y}{8}$$

$$\frac{2y - x}{4} = \frac{4y - 2x}{8}$$

$$\frac{x + y}{8} = \frac{x + y}{8}$$

$$\frac{12x - 16y + 4y - 2x - x - y}{8} = \frac{9x - 13y}{8}$$

The simplified form is  $\boxed{\frac{9x - 13y}{8}}$ .